

$$\textcircled{1.} \int \frac{\cos x}{2 + \sin x} dx = \int \frac{1}{2+y} dy \stackrel{c}{=} \ln|2+y| = \ln(2 + \sin x) \text{ na } \mathbb{R}$$

1. v\u011bta a substitucei:

$$y = \sin x$$

$$dy = \cos x dx$$

$$\textcircled{2.} \int \sqrt{1-x^2} dx = \int \sqrt{1-\sin^2 t} \cos t dt = \int \sqrt{\cos^2 t} \cos t dt$$

Hled\u00e1me prim. fci na $(-1, 1)$.

2. v\u011bta a substitucei:

$$x = \sin t, \quad t \in \left(-\frac{\pi}{2}, \frac{\pi}{2}\right) \dots t = \arcsin x, \quad x \in (-1, 1)$$

$$dx = \cos t dt$$

$$\varphi(t) = \sin t \text{ prost\u00e1 na } \left(-\frac{\pi}{2}, \frac{\pi}{2}\right), \quad \varphi\left(\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)\right) = (-1, 1)$$

$$= \int \cos^2 t dt = \int \frac{1}{2} (1 + \cos 2t) dt \stackrel{c}{=} \frac{1}{2} t + \frac{1}{4} \sin 2t =$$

$$\uparrow$$

$$\cos t > 0 \text{ pro } t \in \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$$

$$= \frac{1}{2} \arcsin x + \frac{1}{4} \sin(2 \arcsin x) \text{ na } (-1, 1)$$